

# Pari-GP reference card

(PARI-GP version 2.15.2)

Note: optional arguments are surrounded by braces {}.

To start the calculator, type its name in the terminal: **gp**

To exit **gp**, type **quit**, **\q**, or **<C-D>** at prompt.

## Help

describe function	?function
extended description	??keyword
list of relevant help topics	???pattern
name of GP-1.39 function <i>f</i> in GP-2.*	whatnow( <i>f</i> )

## Input/Output

previous result, the result before	%, %`, %`` , etc.
<i>n</i> -th result since startup	% <i>n</i>
separate multiple statements on line	;
extend statement on additional lines	\
extend statements on several lines	{ <i>seq</i> <sub>1</sub> ; <i>seq</i> <sub>2</sub> ;}
comment	/* ... */
one-line comment, rest of line ignored	\\ ...

## Metacommands & Defaults

set default <i>d</i> to <i>val</i>	default({ <i>d</i> },{ <i>val</i> })
toggle timer on/off	#
print time for last result	##
print defaults	\d
set debug level to <i>n</i>	\g <i>n</i>
set memory debug level to <i>n</i>	\gm <i>n</i>
set <i>n</i> significant digits / bits	\p <i>n</i> , \pb <i>n</i>
set <i>n</i> terms in series	\ps <i>n</i>
quit GP	\q
print the list of PARI types	\t
print the list of user-defined functions	\u
read file into GP	\r <i>filename</i>
set debuglevel for domain <i>D</i> to <i>n</i>	setdebug( <i>D</i> , <i>n</i> )

## Debugger / break loop

get out of break loop	break or <C-D>
go up/down <i>n</i> frames	dbg_up({ <i>n</i> }), dbg_down
set break point	breakpoint()
examine object <i>o</i>	dbg_x( <i>o</i> )
current error data	dbg_err()
number of objects on heap and their size	getheap()
total size of objects on PARI stack	getstack()

## PARI Types & Input Formats

t_INT. Integers; hex, binary	±31; ±0x1F, ±0b101
t_REAL. Reals	±3.14, 6.022 E23
t_INTMOD. Integers modulo <i>m</i>	Mod( <i>n</i> , <i>m</i> )
t_FRAC. Rational Numbers	<i>n</i> / <i>m</i>
t_FFELT. Elt in finite field <b>F</b> <sub><i>q</i></sub>	ffgen( <i>q</i> , 't)
t_COMPLEX. Complex Numbers	<i>x</i> + <i>y</i> * I
t_PADIC. <i>p</i> -adic Numbers	<i>x</i> + 0( <i>p</i> ^ <i>k</i> )
t_QUAD. Quadratic Numbers	<i>x</i> + <i>y</i> * quadgen( <i>D</i> ,{'w'})
t_POLMOD. Polynomials modulo <i>g</i>	Mod( <i>f</i> , <i>g</i> )
t_POL. Polynomials	<i>a</i> * <i>x</i> ^ <i>n</i> + ... + <i>b</i>
t_SER. Power Series	<i>f</i> + 0( <i>x</i> ^ <i>k</i> )
t_RFRAC. Rational Functions	<i>f</i> / <i>g</i>
t_QFB. Binary quadratic form	Qfb( <i>a</i> , <i>b</i> , <i>c</i> )
t_VEC/t_COL. Row/Column Vectors	[ <i>x</i> , <i>y</i> , <i>z</i> ], [ <i>x</i> , <i>y</i> , <i>z</i> ]'
t_VEC integer range	[1..10]

t_VECSMALL. Vector of small ints	Vecsmall([ <i>x</i> , <i>y</i> , <i>z</i> ])
t_MAT. Matrices	[ <i>a</i> , <i>b</i> ; <i>c</i> , <i>d</i> ]
t_LIST. Lists	List([ <i>x</i> , <i>y</i> , <i>z</i> ])
t_STR. Strings	"abc"
t_INFINITY. ±∞	+oo, -oo

## Reserved Variable Names

$\pi \approx 3.14$ , $\gamma \approx 0.57$ , $C \approx 0.91$ , $I = \sqrt{-1}$	Pi, Euler, Catalan, I
Landau's big-oh notation	O

## Information about an Object, Precision

PARI type of object <i>x</i>	type( <i>x</i> )
length of <i>x</i> / size of <i>x</i> in memory	# <i>x</i> , sizebyte( <i>x</i> )
real precision / bit precision of <i>x</i>	precision( <i>x</i> ), bitprecision( <i>x</i> )
<i>p</i> -adic, series prec. of <i>x</i>	padicprec( <i>x</i> , <i>p</i> ), serprec( <i>x</i> , <i>v</i> )
current dynamic precision	getlocalprec, getlocalbitprec

## Operators

basic operations	+, − , *, / , ^ , sqr
i←i+1, i←i-1, i←i*j, ...	i++, i--, i*=j,...
Euclidean quotient, remainder	<i>x</i> \/ <i>y</i> , <i>x</i> % <i>y</i> , divrem( <i>x</i> , <i>y</i> )
shift <i>x</i> left or right <i>n</i> bits	<i>x</i> << <i>n</i> , <i>x</i> >> <i>n</i> or shift( <i>x</i> ,± <i>n</i> )
multiply by 2 <sup><i>n</i></sup>	shiftmul( <i>x</i> , <i>n</i> )
comparison operators	<=, <, >=, >, ==, !=, ==, lex, cmp
boolean operators (or, and, not)	, &&, !
bit operations	bitand, bitneg, bitor, bitxor, bitnegimply
maximum/minimum of <i>x</i> and <i>y</i>	max( <i>x</i> , <i>y</i> ), min( <i>x</i> , <i>y</i> )
sign of <i>x</i> (gives −1,0,1)	sign( <i>x</i> )
binary exponent of <i>x</i>	exponent( <i>x</i> )
derivative of <i>f</i> , 2nd derivative, etc.	<i>f</i> ' , <i>f</i> '' , ...
differential operator	diffop( <i>f</i> , <i>v</i> , <i>d</i> ,{ <i>n</i> =1})
quote operator (formal variable)	'x
assignment	x = <i>value</i>
simultaneous assignment <i>x</i> ← <i>v</i> [1], <i>y</i> ← <i>v</i> [2]	[x,y] = v

## Select Components

<i>Caveat</i> : components start at index <i>n</i> = 1.	
<i>n</i> -th component of <i>x</i>	component( <i>x</i> , <i>n</i> )
<i>n</i> -th component of vector/list <i>x</i>	<i>x</i> [ <i>n</i> ]
components <i>a</i> , <i>a</i> + 1, ..., <i>b</i> of vector <i>x</i>	<i>x</i> [ <i>a</i> .. <i>b</i> ]
( <i>m</i> , <i>n</i> )-th component of matrix <i>x</i>	<i>x</i> [ <i>m</i> , <i>n</i> ]
row <i>m</i> or column <i>n</i> of matrix <i>x</i>	<i>x</i> [ <i>m</i> ,], <i>x</i> [, <i>n</i> ]
numerator/denominator of <i>x</i>	numerator( <i>x</i> ), denominator( <i>x</i> )

## Random Numbers

random integer/prime in [0, <i>N</i> [	random( <i>N</i> ), randomprime( <i>N</i> )
get/set random seed	getrand, setrand( <i>s</i> )

## Conversions

to vector, matrix, vec. of small ints	Col/Vec, Mat, Vecsmall
to list, set, map, string	List, Set, Map, Str
create ( <i>x</i> mod <i>y</i> )	Mod( <i>x</i> , <i>y</i> )
make <i>x</i> a polynomial of <i>v</i>	Pol( <i>x</i> ,{ <i>v</i> })
variants of Pol <i>et al.</i> , in reverse order	Polrev, Vecrev, Colrev
make <i>x</i> a power series of <i>v</i>	Ser( <i>x</i> ,{ <i>v</i> })
convert <i>x</i> to simplest possible type	simplify( <i>x</i> )
object <i>x</i> with real precision <i>n</i>	precision( <i>x</i> , <i>n</i> )
object <i>x</i> with bit precision <i>n</i>	bitprecision( <i>x</i> , <i>n</i> )
set precision to <i>p</i> digits in dynamic scope	localprec( <i>p</i> )
set precision to <i>p</i> bits in dynamic scope	localbitprec( <i>p</i> )

## Character strings

convert to TeX representation	strtex( <i>x</i> )
string from bytes / from format+args	strchr, sprintf
split string / join strings	strsplit, strjoin
convert time <i>t</i> ms. to h, m, s, ms format	strtime( <i>t</i> )
<b>Conjugates and Lifts</b>	
conjugate of a number <i>x</i>	conj( <i>x</i> )
norm of <i>x</i> , product with conjugate	norm( <i>x</i> )
<i>L</i> <sup><i>p</i></sup> norm of <i>x</i> ( <i>L</i> <sup>∞</sup> if no <i>p</i> )	normlp( <i>x</i> ,{ <i>p</i> })
square of <i>L</i> <sup>2</sup> norm of <i>x</i>	norml2( <i>x</i> )
lift of <i>x</i> from Mods and <i>p</i> -adics	lift, centerlift( <i>x</i> )
recursive lift	liftall
lift all t_INT and t_PADIC (→t_INT)	liftint
lift all t_POLMOD (→t_POL)	liftpol

## Lists, Sets & Maps

<b>Sets</b> (= row vector with strictly increasing entries w.r.t. cmp)	
intersection of sets <i>x</i> and <i>y</i>	setintersect( <i>x</i> , <i>y</i> )
set of elements in <i>x</i> not belonging to <i>y</i>	setminus( <i>x</i> , <i>y</i> )
symmetric difference <i>x</i> Δ <i>y</i>	setdelta( <i>x</i> , <i>y</i> )
union of sets <i>x</i> and <i>y</i>	setunion( <i>x</i> , <i>y</i> )
does <i>y</i> belong to the set <i>x</i>	setsearch( <i>x</i> , <i>y</i> ,{ <i>flag</i> })
set of all <i>f</i> ( <i>x</i> , <i>y</i> ), <i>x</i> ∈ <i>X</i> , <i>y</i> ∈ <i>Y</i>	setbinop( <i>f</i> , <i>X</i> , <i>Y</i> )
is <i>x</i> a set ?	setisset( <i>x</i> )

<b>Lists.</b> create empty list: <i>L</i> = List()	
append <i>x</i> to list <i>L</i>	listput( <i>L</i> , <i>x</i> ,{ <i>i</i> })
remove <i>i</i> -th component from list <i>L</i>	listpop( <i>L</i> ,{ <i>i</i> })
insert <i>x</i> in list <i>L</i> at position <i>i</i>	listinsert( <i>L</i> , <i>x</i> , <i>i</i> )
sort the list <i>L</i> in place	listsort( <i>L</i> ,{ <i>flag</i> })
<b>Maps.</b> create empty dictionary: <i>M</i> = Map()	
attach value <i>v</i> to key <i>k</i>	mapput( <i>M</i> , <i>k</i> , <i>v</i> )
recover value attach to key <i>k</i> or error	mapget( <i>M</i> , <i>k</i> )
is key <i>k</i> in the dict? (set <i>v</i> to <i>M</i> ( <i>k</i> ))	mapisdefined( <i>M</i> , <i>k</i> ,{& <i>v</i> })
remove <i>k</i> from map domain	mapdelete( <i>M</i> , <i>k</i> )

## GP Programming

### User functions and closures

<i>x</i> , <i>y</i> are formal parameters; <i>y</i> defaults to Pi if parameter omitted;	
<i>z</i> , <i>t</i> are local variables (lexical scope), <i>z</i> initialized to 1.	
fun(x, y=Pi) = my(z=1, t); seq	
fun = (x, y=Pi) -> my(z=1, t); seq	
attach help message <i>h</i> to <i>s</i>	addhelp( <i>s</i> , <i>h</i> )
undefine symbol <i>s</i> (also kills help)	kill( <i>s</i> )
<b>Control Statements</b> ( <i>X</i> : formal parameter in expression <i>seq</i> )	
if <i>a</i> ≠ 0, evaluate <i>seq</i> <sub>1</sub> , else <i>seq</i> <sub>2</sub>	if( <i>a</i> ,{ <i>seq</i> <sub>1</sub> },{ <i>seq</i> <sub>2</sub> })
eval. <i>seq</i> for <i>a</i> ≤ <i>X</i> ≤ <i>b</i>	for( <i>X</i> = <i>a</i> , <i>b</i> , <i>seq</i> )
...for <i>X</i> ∈ <i>v</i>	foreach( <i>v</i> , <i>X</i> , <i>seq</i> )
...for primes <i>a</i> ≤ <i>X</i> ≤ <i>b</i>	forprime( <i>X</i> = <i>a</i> , <i>b</i> , <i>seq</i> )
...for primes ≡ <i>a</i> (mod <i>q</i> )	forprimestep( <i>X</i> = <i>a</i> , <i>b</i> , <i>q</i> , <i>seq</i> )
...for composites <i>a</i> ≤ <i>X</i> ≤ <i>b</i>	forcomposite( <i>X</i> = <i>a</i> , <i>b</i> , <i>seq</i> )
...for <i>a</i> ≤ <i>X</i> ≤ <i>b</i> stepping <i>s</i>	forstep( <i>X</i> = <i>a</i> , <i>b</i> , <i>s</i> , <i>seq</i> )
...for <i>X</i> dividing <i>n</i>	fordiv( <i>n</i> , <i>X</i> , <i>seq</i> )
... <i>X</i> = [ <i>n</i> , factor( <i>n</i> )], <i>a</i> ≤ <i>n</i> ≤ <i>b</i>	forfactored( <i>X</i> = <i>a</i> , <i>b</i> , <i>seq</i> )
...as above, <i>n</i> squarefree	forsquarefree( <i>X</i> = <i>a</i> , <i>b</i> , <i>seq</i> )
... <i>X</i> = [ <i>d</i> , factor( <i>d</i> )], <i>d</i>   <i>n</i>	fordivfactored( <i>n</i> , <i>X</i> , <i>seq</i> )
multivariable for, lex ordering	forvec( <i>X</i> = <i>v</i> , <i>seq</i> )

loop over partitions of  $n$   
... permutations of  $S$   
... subsets of  $\{1, \dots, n\}$   
...  $k$ -subsets of  $\{1, \dots, n\}$   
... vectors  $v$ ,  $q(v) \leq B$ ;  $q > 0$   
...  $H < G$  finite abelian group  
evaluate  $seq$  until  $a \neq 0$   
while  $a \neq 0$ , evaluate  $seq$   
exit  $n$  innermost enclosing loops  
start new iteration of  $n$ -th enclosing loop  
return  $x$  from current subroutine

**Exceptions, warnings**  
raise an exception / warning  
type of error message  $E$   
try  $seq_1$ , evaluate  $seq_2$  on error

**Functions with closure arguments / results**  
number of arguments of  $f$   
select from  $v$  according to  $f$   
apply  $f$  to all entries in  $v$   
evaluate  $f(a_1, \dots, a_n)$   
evaluate  $f(\dots f(f(a_1, a_2), a_3) \dots, a_n)$   
calling function as closure

**Sums & Products**  
sum  $X = a$  to  $X = b$ , initialized at  $x$   
sum entries of vector  $v$   
product of all vector entries  
sum  $expr$  over divisors of  $n$   
... assuming  $expr$  multiplicative  
product  $a \leq X \leq b$ , initialized at  $x$   
product over primes  $a \leq X \leq b$

**Sorting**  
sort  $x$  by  $k$ -th component  
min.  $m$  of  $x$  ( $m = x[i]$ ), max.  
does  $y$  belong to  $x$ , sorted wrt.  $f$   
 $\prod g^x \rightarrow$  factorization ( $\Rightarrow$  sorted, unique  $g$ )

**Input/Output**  
print with/without  $\backslash n$ ,  $\text{\TeX}$  format  
pretty print matrix  
print fields with separator  
formatted printing  
write  $args$  to file  
write  $x$  in binary format  
read file into GP  
... return as vector of lines  
... return as vector of strings  
read a string from keyboard

**Files and file descriptors**  
File descriptors allow efficient small consecutive reads or writes from or to a given file. The argument  $n$  below is always a descriptor, attached to a file in **r**(ead), **w**(rite) or **a**(ppend) mode.  
get descriptor  $n$  for file  $path$  in given  $mode$   
... from shell  $cmd$  output (pipe)

close descriptor  
commit pending write operations  
read logical line from file  
... raw line from file  
write  $s \backslash n$  to file  
... write  $s$  to file

forpart( $p = n, seq$ )  
forperm( $S, p, seq$ )  
forsubset( $n, p, seq$ )  
forsubset( $[n, k], p, seq$ )  
forqfvec( $v, q, b, seq$ )  
forsubgroup( $H = G$ )  
until( $a, seq$ )  
while( $a, seq$ )  
break( $\{n\}$ )  
next( $\{n\}$ )  
return( $\{x\}$ )

error(), warning()  
errname( $E$ )  
iferr( $seq_1, E, seq_2$ )

arity( $f$ )  
select( $f, v$ )  
apply( $f, v$ )  
call( $f, a$ )  
fold( $f, a$ )  
self()

sum( $X = a, b, expr, \{x\}$ )  
vecsum( $v$ )  
vecprod( $v$ )  
sumdiv( $n, X, expr$ )  
sumdivmult( $n, X, expr$ )  
prod( $X = a, b, expr, \{x\}$ )  
prodeuler( $X = a, b, expr$ )

vecsrt( $x, \{k\}, \{fl = 0\}$ )  
vecmin( $x, \{\&i\}$ ), vecmax  
vecsearch( $x, y, \{f\}$ )  
matreduce( $m$ )

print, print1, printtex  
printp  
printsep( $sep, \dots$ ), printsep1  
printf()  
write, write1, writetex( $file, args$ )  
writebin( $file, x$ )  
read( $\{file\}$ )  
readvec( $\{file\}$ )  
readstr( $\{file\}$ )  
input()

# Pari-GP reference card

(PARI-GP version 2.15.2)

## Timers

CPU time in  $ms$  and reset timer  
CPU time in  $ms$  since gp startup  
time in  $ms$  since UNIX Epoch  
timeout command after  $s$  seconds

## Interface with system

allocates a new stack of  $s$  bytes  
alias  $old$  to  $new$   
install function from library  
execute system command  $a$   
... and feed result to GP  
... returning GP string  
get \$VAR from environment  
expand env. variable in string

## Parallel evaluation

These functions evaluate their arguments in parallel (pthreads or MPI); args. must not access global variables (use export for this) and must be free of side effects. Enabled if threading engine is not *single* in gp header.

evaluate  $f$  on  $x[1], \dots, x[n]$   
evaluate closures  $f[1], \dots, f[n]$   
as select  
as sum  
as vector  
eval  $f$  for  $i = a, \dots, b$   
... for each element  $x$  in  $v$   
... for  $p$  prime in  $[a, b]$   
... for  $p = a \bmod q$   
... multivariate  
export  $x$  to parallel world  
... all dynamic variables  
frees exported value  $x$   
... all exported values

## Linear Algebra

dimensions of matrix  $x$   
multiply two matrices  
... assuming result is diagonal  
concatenation of  $x$  and  $y$   
extract components of  $x$   
transpose of vector or matrix  $x$   
adjoint of the matrix  $x$   
eigenvectors/values of matrix  $x$   
characteristic/minimal polynomial of  $x$   
trace/determinant of matrix  $x$   
permanent of matrix  $x$   
Frobenius form of  $x$   
QR decomposition  
apply matqr's transform to  $v$

## Constructors & Special Matrices

$\{g(x): x \in v \text{ s.t. } f(x)\}$   
 $\{x: x \in v \text{ s.t. } f(x)\}$   
 $\{g(x): x \in v\}$   
row vec. of  $expr$  eval'ed at  $1 \leq i \leq n$   
col. vec. of  $expr$  eval'ed at  $1 \leq i \leq n$   
vector of small ints

gettime()  
getabstime()  
getwalltime()  
alarm( $s, expr$ )  
allocatemem( $\{s\}$ )  
alias( $new, old$ )  
install( $f, code, \{gpf\}, \{lib\}$ )  
system( $a$ )  
extern( $a$ )  
externstr( $a$ )  
getenv("VAR")  
strexpand( $x$ )

parapply( $f, x$ )  
pareval( $f$ )  
parselect( $f, A, \{flag\}$ )  
parsum( $i = a, b, expr$ )  
parvector( $n, i, \{expr\}$ )  
parfor( $i = a, \{b\}, f, \{r\}, \{f_2\}$ )  
parforeach( $v, x, f, \{r\}, \{f_2\}$ )  
parforprime( $p = a, \{b\}, f, \{r\}, \{f_2\}$ )  
parforprimestep( $p = a, \{b\}, q, f, \{r\}, \{f_2\}$ )  
parforvec( $X = v, f, \{r\}, \{f_2\}, \{flag\}$ )  
export( $x$ )  
exportall()  
unexport( $x$ )  
unexportall()

matsize( $x$ )  
 $x * y$   
matmultodiagonal( $x, y$ )  
concat( $x, \{y\}$ )  
vecextract( $x, y, \{z\}$ )  
 $x \sim$ , mattranspose( $x$ )  
matadjoint( $x$ )  
mateigen( $x$ )  
charpoly( $x$ ), minpoly( $x$ )  
trace( $x$ ), matdet( $x$ )  
matpermanent( $x$ )  
matfrobenius( $x$ )  
matqr( $x$ )  
mathouseholder( $Q, v$ )

$[g(x) \mid x \leftarrow v, f(x)]$   
 $[x \mid x \leftarrow v, f(x)]$   
 $[g(x) \mid x \leftarrow v]$   
vector( $n, \{i\}, \{expr\}$ )  
vectorv( $n, \{i\}, \{expr\}$ )  
vectorsmall( $n, \{i\}, \{expr\}$ )

$[c, c \cdot x, \dots, c \cdot x^n]$   
 $[1, 2^x, \dots, n^x]$   
matrix  $1 \leq i \leq m, 1 \leq j \leq n$   
define matrix by blocks  
diagonal matrix with diagonal  $x$   
is  $x$  diagonal?  
 $x \cdot \text{matdiagonal}(d)$   
 $n \times n$  identity matrix  
Hessenberg form of square matrix  $x$   
 $n \times n$  Hilbert matrix  $H_{ij} = (i + j - 1)^{-1}$   
 $n \times n$  Pascal triangle  
companion matrix to polynomial  $x$   
Sylvester matrix of  $x$  and  $y$

## Gaussian elimination

kernel of matrix  $x$   
intersection of column spaces of  $x$  and  $y$   
solve  $MX = B$  ( $M$  invertible)  
one sol of  $M * X = B$   
basis for image of matrix  $x$   
columns of  $x$  not in **matimage**  
supplement columns of  $x$  to get basis  
rows, cols to extract invertible matrix  
rank of the matrix  $x$   
solve  $MX = B \bmod D$   
image mod  $D$   
kernel mod  $D$   
inverse mod  $D$   
determinant mod  $D$

## Lattices & Quadratic Forms

### Quadratic forms

evaluate  ${}^t x Q y$   
evaluate  ${}^t x Q x$   
signature of quad form  ${}^t y * x * y$   
decomp into squares of  ${}^t y * x * y$   
eigenvalues/vectors for real symmetric  $x$

### HNF and SNF

upper triangular Hermite Normal Form  
HNF of  $x$  where  $d$  is a multiple of  $\det(x)$   
multiple of  $\det(x)$   
HNF of  $(x \mid \text{diagonal}(D))$   
elementary divisors of  $x$   
 $q$ -rank from elementary divisors  
elementary divisors of  $\mathbf{Z}[a]/(f'(a))$   
integer kernel of  $x$   
 $\mathbf{Z}$ -module  $\leftrightarrow$   $\mathbf{Q}$ -vector space

### Lattices

LLL-algorithm applied to columns of  $x$   
... for Gram matrix of lattice  
find up to  $m$  sols of  $\mathbf{qfnorm}(x, y) \leq b$   
 $v, v[i] :=$  number of  $y$  s.t.  $\mathbf{qfnorm}(x, y) = i$   
perfection rank of  $x$   
find isomorphism between  $q$  and  $Q$   
precompute for isomorphism test with  $q$   
automorphism group of  $q$

Based on an earlier version by Joseph H. Silverman  
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Send comments and corrections to (Karim.Belabas@math.u-bordeaux.fr)

convert **qfauto** for GAP/Magma      **qfautoexport**( $G, \{flag\}$ )  
orbits of  $V$  under  $G \subset \mathrm{GL}(V)$       **qforbits**( $G, V$ )

**Polynomials & Rational Functions**

all defined polynomial variables      **variables**()  
get var. of highest priority (higher than  $v$ )      **varhigher**( $name, \{v\}$ )  
... of lowest priority (lower than  $v$ )      **varlower**( $name, \{v\}$ )

**Coefficients, variables and basic operators**

degree of  $f$       **poldegree**( $f$ )  
coef. of degree  $n$  of  $f$ , leading coef.      **polcoef**( $f, n$ ), **pollead**  
main variable / all variables in  $f$       **variable**( $f$ ), **variables**( $f$ )  
replace  $x$  by  $y$  in  $f$       **subst**( $f, x, y$ )  
evaluate  $f$  replacing vars by their value      **eval**( $f$ )  
replace polynomial expr.  $T(x)$  by  $y$  in  $f$       **substpol**( $f, T, y$ )  
replace  $x_1, \dots, x_n$  by  $y_1, \dots, y_n$  in  $f$       **substvec**( $f, x, y$ )

$f \in A[x]$ ; reciprocal polynomial  $x^{\deg f} f\left(\frac{1}{x}\right)$       **polrecip**( $f$ )  
gcd of coefficients of  $f$       **content**( $f$ )  
derivative of  $f$  w.r.t.  $x$       **deriv**( $f, \{x\}$ )  
...  $n$ -th derivative of  $f$       **derivn**( $f, n, \{x\}$ )  
formal integral of  $f$  w.r.t.  $x$       **intformal**( $f, \{x\}$ )  
formal sum of  $f$  w.r.t.  $x$       **sumformal**( $f, \{x\}$ )

**Constructors & Special Polynomials**

interpolation polynomial at  $(x[1], y[1]), \dots, (x[n], y[n])$ , evaluated at  $t$ , with error estimate  $e$       **polinterpolate**( $x, \{y\}, \{t\}, \{&e\}$ )  
 $T_n/U_n, H_n$       **polchebyshev**( $n$ ), **polhermite**( $n$ )  
 $P_n, L_n^{(\alpha)}$       **pollegendre**( $n$ ), **pollaguerre**( $n, a$ )  
 $n$ -th cyclotomic polynomial  $\Phi_n$       **polcyclo**( $n$ )  
return  $n$  if  $f = \Phi_n$ , else 0      **poliscyclo**( $f$ )  
is  $f$  a product of cyclotomic polynomials?      **poliscycloprod**( $f$ )  
Zagier's polynomial of index  $(n, m)$       **polzagier**( $n, m$ )

**Resultant, elimination**

discriminant of polynomial  $f$       **poldisc**( $f$ )  
find factors of **poldisc**( $f$ )      **poldiscfactors**( $f$ )  
resultant  $R = \mathrm{Res}_v(f, g)$       **polresultant**( $f, g, \{v\}$ )  
 $[u, v, R], xu + yv = \mathrm{Res}_v(f, g)$       **polresultanttext**( $x, y, \{v\}$ )  
solve Thue equation  $f(x, y) = a$       **thue**( $t, a, \{sol\}$ )  
initialize  $t$  for Thue equation solver      **thueinit**( $f$ )

**Roots and Factorization (Complex/Real)**

complex roots of  $f$       **polroots**( $f$ )  
bound complex roots of  $f$       **polrootsbound**( $f$ )  
number of real roots of  $f$  (in  $[a, b]$ )      **polsturm**( $f, \{[a, b]\}$ )  
real roots of  $f$  (in  $[a, b]$ )      **polrootsreal**( $f, \{[a, b]\}$ )  
complex embeddings of **t\_POLMOD**  $z$       **conjsvec**( $z$ )

**Roots and Factorization (Finite fields)**

factor  $f$  mod  $p$ , roots      **factormod**( $f, p$ ), **polrootsmod**  
factor  $f$  over  $\mathbf{F}_p[x]/(T)$ , roots      **factormod**( $f, [T, p]$ ), **polrootsmod**  
squarefree factorization of  $f$  in  $\mathbf{F}_q[x]$       **factormodSQF**( $f, \{D\}$ )  
distinct degree factorization of  $f$  in  $\mathbf{F}_q[x]$       **factormodDDF**( $f, \{D\}$ )  
factor  $n$ -th cyclotomic pol.  $\Phi_n$  mod  $p$       **factormodcyclo**( $n, p$ )

**Roots and Factorization ( $p$ -adic fields)**

factor  $f$  over  $\mathbf{Q}_p$ , roots      **factorpadic**( $f, p, r$ ), **polrootspadic**  
 $p$ -adic root of  $f$  congruent to  $a$  mod  $p$       **padicappr**( $f, a$ )  
Newton polygon of  $f$  for prime  $p$       **newtonpoly**( $f, p$ )  
Hensel lift  $A/\mathrm{lc}(A) = \prod_i B[i] \bmod p^e$       **polhensellift**( $A, B, p, e$ )  
 $T = \prod (x - z_i) \mapsto \prod [x - \omega(z_i)] \in \mathbf{Z}_p[x]$       **polteichmuller**( $T, p, e$ )  
extensions of  $\mathbf{Q}_p$  of degree  $N$       **padicfields**( $p, N$ )

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**Roots and Factorization (Miscellaneous)**

symmetric powers of roots of  $f$  up to  $n$       **polsym**( $f, n$ )  
Graeffe transform of  $f, g(x^2) = f(x)f(-x)$       **polgraeffe**( $f$ )  
factor  $f$  over coefficient field      **factor**( $f$ )  
cyclotomic factors of  $f \in \mathbf{Q}[X]$       **polcyclofactors**( $f$ )

**Finite Fields**

A finite field is encoded by any element (**t\_FFELT**).  
find irreducible  $T \in \mathbf{F}_p[x]$ ,  $\deg T = n$       **ffinit**( $p, n, \{x\}$ )  
Create  $t$  in  $\mathbf{F}_q \simeq \mathbf{F}_p[t]/(T)$       **t = ffgn**( $T, 't$ )  
... indirectly, with implicit  $T$       **t = ffgn**( $q, 't$ ); **T = t.mod**  
map  $m$  from  $\mathbf{F}_q \ni a$  to  $\mathbf{F}_{q^k} \ni b$       **m = ffbend**( $a, b$ )  
build  $K = \mathbf{F}_q[x]/(P)$  extending  $\mathbf{F}_q \ni a$ ,      **ffextend**( $a, P$ )  
evaluate map  $m$  on  $x$       **ffmap**( $m, x$ )  
inverse map of  $m$       **ffinvmap**( $m$ )  
compose maps  $m \circ n$       **ffcompomap**( $m, n$ )  
 $x$  as polmod over codomain of map  $m$       **ffmaprel**( $m, x$ )  
 $F^n$  over  $\mathbf{F}_q \ni a$       **fffrobenius**( $a, n$ )  
 $\#\{\text{monic irred. } T \in \mathbf{F}_q[x], \deg T = n\}$       **ffnbirred**( $q, n$ )

**Formal & p-adic Series**

truncate power series or  $p$ -adic number      **truncate**( $x$ )  
valuation of  $x$  at  $p$       **valuation**( $x, p$ )  
**Dirichlet and Power Series**  
Taylor expansion around 0 of  $f$  w.r.t.  $x$       **taylor**( $f, x$ )  
Laurent series of closure  $F$  up to  $x^k$       **laurentseries**( $f, k$ )  
 $\sum a_k b_k t^k$  from  $\sum a_k t^k$  and  $\sum b_k t^k$       **serconvol**( $a, b$ )  
 $f = \sum a_k t^k$  from  $\sum (a_k/k!) t^k$       **serlaplace**( $f$ )  
reverse power series  $F$  so  $F(f(x)) = x$       **serreverse**( $f$ )  
remove terms of degree  $< n$  in  $f$       **serchop**( $f, n$ )  
Dirichlet series multiplication / division      **dirmul, dirdiv**( $x, y$ )  
Dirichlet Euler product ( $b$  terms)      **direuler**( $p = a, b, expr$ )

**Transcendental and  $p$ -adic Functions**

real, imaginary part of  $x$       **real**( $x$ ), **imag**( $x$ )  
absolute value, argument of  $x$       **abs**( $x$ ), **arg**( $x$ )  
square/nth root of  $x$       **sqrt**( $x$ ), **sqrtn**( $x, n, \{&z\}$ )  
all  $n$ -th roots of 1      **rootsof1**( $n$ )  
FFT of  $[f_0, \dots, f_{n-1}]$       **w = fftinit**( $n$ ), **fft/fftin**( $w, f$ )  
trig functions      **sin, cos, tan, cotan, sinc**  
inverse trig functions      **asin, acos, atan**  
hyperbolic functions      **sinh, cosh, tanh, cotanh**  
inverse hyperbolic functions      **asinh, acosh, atanh**  
 $\log(x), \log(1+x), e^x, e^x - 1$       **log, loglp, exp, expm1**  
Euler  $\Gamma$  function,  $\log \Gamma, \Gamma'/\Gamma$       **gamma, lngamma, psi**  
half-integer gamma function  $\Gamma(n + 1/2)$       **gammah**( $n$ )  
Riemann's zeta  $\zeta(s) = \sum n^{-s}$       **zeta**( $s$ )  
 $\sum_{1 \leq n \leq N} n^s$       **dirpowerssum**( $N, s$ )  
Hurwitz's  $\zeta(s, x) = \sum (n+x)^{-s}$       **zetahurwitz**( $s, x$ )  
Lerch  $\Phi(z, s, x) = \sum z^n (n+x)^{-s}$       **lerchphi**( $z, s, x$ )  
Lerch  $L(s, x, t) = \Phi(e^{2i\pi t}, s, x)$       **lerchzeta**( $s, x, t$ )  
multiple zeta value (MZV),  $\zeta(s_1, \dots, s_k)$       **zetamult**( $s, \{T\}$ )  
all MZVs for weight  $\sum s_i = n$       **zetamultall**( $n$ )  
convert MZV id to  $[s_1, \dots, s_k]$       **zetamultconvert**( $f, \{flag\}$ )  
MZV dual sequence      **zetamultdual**( $s$ )  
multiple polylog  $Li_{s_1, \dots, s_k}(z_1, \dots, z_k)$       **polylogmult**( $s, z$ )

incomplete  $\Gamma$  function ( $y = \Gamma(s)$ )      **incgam**( $s, x, \{y\}$ )  
complementary incomplete  $\Gamma$       **incgamc**( $s, x$ )  
 $\int_x^\infty e^{-t} dt/t, (2/\sqrt{\pi}) \int_x^\infty e^{-t^2} dt$       **eint1, erfc**  
elliptic integral of 1st and 2nd kind      **ellK**( $k$ ), **ellE**( $k$ )  
dilogarithm of  $x$       **dilog**( $x$ )  
 $m$ -th polylogarithm of  $x$       **polylog**( $m, x, \{flag\}$ )  
 $U$ -confluent hypergeometric function      **hyperu**( $a, b, u$ )  
Hypergeometric  ${}_pF_q(A, B; z)$       **hypergeom**( $A, B, z$ )  
Bessel  $J_n(x), J_{n+1/2}(x)$       **besselj**( $n, x$ ), **besseljh**( $n, x$ )  
Bessel  $I_\nu, K_\nu, H_\nu^1, H_\nu^2, Y_\nu$       **(bessel)i, k, h1, h2, y**  
 $k$ -th zero of  $J_\nu(x)$       **besseljzero**( $nu, \{k = 1\}$ )  
 $k$ -th zero of  $Y_\nu(x)$       **besselyzero**( $nu, \{k = 1\}$ )  
Airy functions  $A_i(x), B_i(x)$       **airy**( $x$ )  
Lambert  $W: x$  s.t.  $xe^x = y$       **lambertw**( $y$ )  
Teichmuller character of  $p$ -adic  $x$       **teichmuller**( $x$ )

**Iterations, Sums & Products**

**Numerical integration for meromorphic functions**

Behaviour at endpoint for Double Exponential (DE) methods: either a scalar ( $a \in \mathbf{C}$ , regular) or  $\pm\infty$  (decreasing at least as  $x^{-2}$ ) or  
 $(x-a)^{-\alpha}$  singularity      **[a, a]**  
exponential decrease  $e^{-\alpha|x|}$       **[ $\pm\infty, a$ ],  $\alpha > 0$**   
slow decrease  $|x|^\alpha$       **...  $\alpha < -1$**   
oscillating as  $\cos(kx)$        **$\alpha = kI, k > 0$**   
oscillating as  $\sin(kx)$        **$\alpha = -kI, k > 0$**

numerical integration      **intnum**( $x = a, b, f, \{T\}$ )  
weights  $T$  for **intnum**      **intnuminit**( $a, b, \{m\}$ )  
weights  $T$  incl. kernel  $K$       **intfuncinit**( $t = a, b, K, \{m\}$ )  
integrate  $(2i\pi)^{-1} f$  on circle  $|z-a| = R$       **intcirc**( $x = a, R, f, \{T\}$ )

**Other integration methods**

$n$ -point Gauss-Legendre      **intnumgauss**( $x = a, b, f, \{n\}$ )  
weights for  $n$ -point Gauss-Legendre      **intnumgaussinit**( $\{n\}$ )  
quasi-periodic function, period  $2H$       **intnumosc**( $x = a, f, H$ )  
Romberg (low accuracy)      **intnumromb**( $x = a, b, f, \{flag\}$ )

**Numerical summation**

sum of series  $f(n), n \geq a$  (low accuracy)      **suminf**( $n = a, expr$ )  
sum of alternating/positive series      **sumalt, sumpos**  
sum of series using Euler-Maclaurin      **sumnum**( $n = a, f, \{T\}$ )  
... Sidi summation      **sumnumsidi**( $n = a, f$ )  
 $\sum_{n \geq a} F(n)$ ,  $F$  rational function      **sumnumrat**( $F, a$ )  
...  $\sum_{p \geq a} F(p^s)$       **sumeulerrat**( $F, \{s = 1\}, \{a = 2\}$ )  
weights for **sumnum**,  $a$  as in DE      **sumnuminit**( $\{\infty, a\}$ )  
sum of series by Monien summation      **sumnummonien**( $n = a, f, \{T\}$ )  
weights for **sumnummonien**      **sumnummonieninit**( $\{\infty, a\}$ )  
sum of series using Abel-Plana      **sumnumap**( $n = a, f, \{T\}$ )  
weights for **sumnumap**,  $a$  as in DE      **sumnumapinit**( $\{\infty, a\}$ )  
sum of series using Lagrange      **sumnumlagrange**( $n = a, f, \{T\}$ )  
weights for **sumnumlagrange**      **sumnumlagrangeinit**

**Products**

product  $a \leq X \leq b$ , initialized at  $x$       **prod**( $X = a, b, expr, \{x\}$ )  
product over primes  $a \leq X \leq b$       **prodeuler**( $X = a, b, expr$ )  
infinite product  $a \leq X \leq \infty$       **prodinf**( $X = a, expr$ )  
 $\prod_{n \geq a} F(n)$ ,  $F$  rational function      **prodnumrat**( $F, a$ )  
 $\prod_{p \geq a} F(p^s)$       **prodeulerrat**( $F, \{s = 1\}, \{a = 2\}$ )

Other numerical methods

real root of $f$ in $[a, b]$ ; bracketed root	<code>solve(<math>X = a, b, f</math>)</code>
...interval splitting, step $s$	<code>solvestep(<math>X = a, b, s, f, \{flag = 0\}</math>)</code>
limit of $f(t)$ , $t \rightarrow \infty$	<code>limitnum(<math>f, \{\alpha\}</math>)</code>
asymptotic expansion of $f$ (rational)	<code>asypnum(<math>f, \{\alpha\}</math>)</code>
... $N + 1$ terms as floats	<code>asypnumraw(<math>f, N, \{\alpha\}</math>)</code>
numerical derivation w.r.t $x$ : $f'(a)$	<code>derivnum(<math>x = a, f</math>)</code>
evaluate continued fraction $F$ at $t$	<code>contfraceval(<math>F, t, \{L\}</math>)</code>
power series to cont. fraction ( $L$ terms)	<code>contfracinit(<math>S, \{L\}</math>)</code>
Padé approximant (deg. denom. $\leq B$ )	<code>bestapprPade(<math>S, \{B\}</math>)</code>

Elementary Arithmetic Functions

vector of binary digits of $ x $	<code>binary(<math>x</math>)</code>
bit number $n$ of integer $x$	<code>bittest(<math>x, n</math>)</code>
Hamming weight of integer $x$	<code>hammingweight(<math>x</math>)</code>
digits of integer $x$ in base $B$	<code>digits(<math>x, \{B = 10\}</math>)</code>
sum of digits of integer $x$ in base $B$	<code>sumdigits(<math>x, \{B = 10\}</math>)</code>
integer from digits	<code>fromdigits(<math>v, \{B = 10\}</math>)</code>
ceiling/floor/fractional part	<code>ceil, floor, frac</code>
round $x$ to nearest integer	<code>round(<math>x, \{\&amp;e\}</math>)</code>
truncate $x$	<code>truncate(<math>x, \{\&amp;e\}</math>)</code>
gcd/LCM of $x$ and $y$	<code>gcd(<math>x, y</math>), lcm(<math>x, y</math>)</code>
gcd of entries of a vector/matrix	<code>content(<math>x</math>)</code>

Primes and Factorization

extra prime table	<code>addprimes()</code>
add primes in $v$ to prime table	<code>addprimes(<math>v</math>)</code>
remove primes from prime table	<code>removeprimes(<math>v</math>)</code>
Chebyshev $\pi(x)$ , $n$ -th prime $p_n$	<code>primepi(<math>x</math>), prime(<math>n</math>)</code>
vector of first $n$ primes	<code>primes(<math>n</math>)</code>
smallest prime $\geq x$	<code>nextprime(<math>x</math>)</code>
largest prime $\leq x$	<code>precprime(<math>x</math>)</code>
factorization of $x$	<code>factor(<math>x, \{lim\}</math>)</code>
...selecting specific algorithms	<code>factorint(<math>x, \{flag = 0\}</math>)</code>
$n = df^2$ , $d$ squarefree/fundamental	<code>core(<math>n, \{fl\}</math>), coredisc</code>
certificate for (prime) $N$	<code>primecert(<math>N</math>)</code>
verifies a certificate $c$	<code>primecertisvalid(<math>c</math>)</code>
convert certificate to Magma/PRIMO	<code>primecertexport</code>
recover $x$ from its factorization	<code>factorback(<math>f, \{e\}</math>)</code>
$x \in \mathbf{Z}$ , $ x  \leq X$ , $\gcd(N, P(x)) \geq N$	<code>zncoppersmith(<math>P, N, X, \{B\}</math>)</code>
divisors of $N$ in residue class $r$ mod $s$	<code>divisorslensstra(<math>N, r, s</math>)</code>

Divisors and multiplicative functions

number of prime divisors $\omega(n)$ / $\Omega(n)$	<code>omega(<math>n</math>), bigomega</code>
divisors of $n$ / number of divisors $\tau(n)$	<code>divisors(<math>n</math>), numdiv</code>
sum of ( $k$ -th powers of) divisors of $n$	<code>sigma(<math>n, \{k\}</math>)</code>
Möbius $\mu$ -function	<code>moebius(<math>x</math>)</code>
Ramanujan's $\tau$ -function	<code>ramanujantau(<math>x</math>)</code>

Combinatorics

factorial of $x$	<code>x!</code> or <code>factorial(<math>x</math>)</code>
binomial coefficient $\binom{x}{k}$	<code>binomial(<math>x, \{k\}</math>)</code>
Bernoulli number $B_n$ as real/rational	<code>bernreal(<math>n</math>), bernfrac</code>
$[B_0, B_2, \dots B_{2k}]$	<code>bernvec(<math>k</math>)</code>
Bernoulli polynomial $B_n(x)$	<code>bernpol(<math>n, \{x\}</math>)</code>
Euler numbers	<code>eulerfrac, eulerreal, eulervec</code>
Euler polynomial $E_n(x)$	<code>eulerpol(<math>n, \{x\}</math>)</code>
Eulerian polynomial $A_n(x)$	<code>eulerianpol</code>
Fibonacci number $F_n$	<code>fibonacci(<math>n</math>)</code>
Harmonic number $H_{n,r} = 1^{-r} + \dots + n^{-r}$	<code>harmonic(<math>n, r</math>)</code>
Stirling numbers $s(n, k)$ and $S(n, k)$	<code>stirling(<math>n, k, \{flag\}</math>)</code>

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number of partitions of $n$	<code>numbpart(<math>n</math>)</code>
$k$ -th permutation on $n$ letters	<code>numtoperm(<math>n, k</math>)</code>
...index $k$ of permutation $v$	<code>permtotnum(<math>v</math>)</code>
order of permutation $p$	<code>permorder(<math>p</math>)</code>
signature of permutation $p$	<code>permsign(<math>p</math>)</code>
cyclic decomposition of permutation $p$	<code>permcycles(<math>p</math>)</code>

Multiplicative groups  $(\mathbf{Z}/N\mathbf{Z})^*$ ,  $\mathbf{F}_q^*$

Euler $\phi$ -function	<code>eulerphi(<math>x</math>)</code>
multiplicative order of $x$ (divides $\phi$ )	<code>znorder(<math>x, \{o\}</math>), fforder</code>
primitive root mod $q$ / $x$ .mod	<code>znprimroot(<math>q</math>), ffpriroot(<math>x</math>)</code>
structure of $(\mathbf{Z}/n\mathbf{Z})^*$	<code>znstar(<math>n</math>)</code>
discrete logarithm of $x$ in base $g$	<code>znlog(<math>x, g, \{o\}</math>), ffflog</code>
Kronecker-Legendre symbol $(\frac{x}{y})$	<code>kronecker(<math>x, y</math>)</code>
quadratic Hilbert symbol (at $p$ )	<code>hilbert(<math>x, y, \{p\}</math>)</code>

Euclidean algorithm, continued fractions

CRT: solve $z \equiv x$ and $z \equiv y$	<code>chinese(<math>x, y</math>)</code>
minimal $u, v$ so $xu + yv = \gcd(x, y)$	<code>gcdext(<math>x, y</math>)</code>
half-gcd algorithm	<code>halfgcd(<math>x, y</math>)</code>
continued fraction of $x$	<code>contfrac(<math>x, \{b\}, \{lmax\}</math>)</code>
last convergent of continued fraction $x$	<code>contfracpnqn(<math>x</math>)</code>
rational approximation to $x$ (den. $\leq B$ )	<code>bestappr(<math>x, \{B\}</math>)</code>
recognize $x \in \mathbf{C}$ as polmod mod $T \in \mathbf{Z}[X]$	<code>bestapprnf(<math>x, T</math>)</code>

Miscellaneous

integer square / $n$ -th root of $x$	<code>sqrtnint(<math>x, n</math>)</code>
largest integer $e$ s.t. $b^e \leq x$ , $e = \lfloor \log_b(x) \rfloor$	<code>logint(<math>x, b, \{\&amp;z\}</math>)</code>

Characters

Let  $\chi = [d_1, \dots, d_k]$  represent an abelian group  $G = \oplus (\mathbf{Z}/d_j\mathbf{Z}) \cdot g_j$  or any structure  $G$  affording a `.cyc` method; e.g. `znstar( $q, 1$ )` for Dirichlet characters. A character  $\chi$  is coded by  $[c_1, \dots, c_k]$  such that  $\chi(g_j) = e(n_j/d_j)$ .  
 $\chi \cdot \psi$ ;  $\chi^{-1}$ ;  $\chi \cdot \psi^{-1}$ ;  $\chi^k$       `charmul, charconj, chardiv, charpow`  
order of  $\chi$       `charorder( $cyc, \chi$ )`  
kernel of  $\chi$       `charker( $cyc, \chi$ )`  
 $\chi(x)$ ,  $G$  a GP group structure      `chareval( $G, \chi, x, \{z\}$ )`  
Galois orbits of characters      `chargalois( $G$ )`

Dirichlet Characters

initialize $G = (\mathbf{Z}/q\mathbf{Z})^*$	<code>G = znstar(<math>q, 1</math>)</code>
convert datum $D$ to $[G, \chi]$	<code>znchar(<math>D</math>)</code>
is $\chi$ odd?	<code>zncharisodd(<math>G, \chi</math>)</code>
real $\chi \rightarrow$ Kronecker symbol $(D/\cdot)$	<code>znchartokronecker(<math>G, \chi</math>)</code>
conductor of $\chi$	<code>zncharconductor(<math>G, \chi</math>)</code>
$[G_0, \chi_0]$ primitive attached to $\chi$	<code>znchartoprimitive(<math>G, \chi</math>)</code>
induce $\chi \in \hat{G}$ to $\mathbf{Z}/N\mathbf{Z}$	<code>zncharinduce(<math>G, \chi, N</math>)</code>
$\chi p$	<code>znchardecompose(<math>G, \chi, p</math>)</code>
$\prod_p  (\chi, N)  \chi p$	<code>znchardecompose(<math>G, \chi, Q</math>)</code>
complex Gauss sum $G_a(\chi)$	<code>znchargauss(<math>G, \chi</math>)</code>

Conrey labelling

Conrey label $m \in (\mathbf{Z}/q\mathbf{Z})^* \rightarrow$ character	<code>znconreychar(<math>G, m</math>)</code>
character $\rightarrow$ Conrey label	<code>znconreyexp(<math>G, \chi</math>)</code>
log on Conrey generators	<code>znconreylog(<math>G, m</math>)</code>
conductor of $\chi$ ( $\chi_0$ primitive)	<code>znconreyconductor(<math>G, \chi, \{\chi_0\}</math>)</code>

True-False Tests

is $x$ the disc. of a quadratic field?	<code>isfundamental(<math>x</math>)</code>
is $x$ a prime?	<code>isprime(<math>x</math>)</code>
is $x$ a strong pseudo-prime?	<code>ispseudoprime(<math>x</math>)</code>
is $x$ square-free?	<code>issquarefree(<math>x</math>)</code>
is $x$ a square?	<code>issquare(<math>x, \{\&amp;n\}</math>)</code>
is $x$ a perfect power?	<code>ispower(<math>x, \{k\}, \{\&amp;n\}</math>)</code>
is $x$ a perfect power of a prime? ( $x = p^n$ )	<code>isprimepower(<math>x, \&amp;n</math>)</code>
... of a pseudoprime?	<code>ispseudoprimepower(<math>x, \&amp;n</math>)</code>
is $x$ powerful?	<code>ispowerful(<math>x</math>)</code>
is $x$ a totient? ( $x = \varphi(n)$ )	<code>istotient(<math>x, \{\&amp;n\}</math>)</code>
is $x$ a polygonal number? ( $x = P(s, n)$ )	<code>ispolygonal(<math>x, s, \{\&amp;n\}</math>)</code>
is $pol$ irreducible?	<code>polisirreducible(<math>pol</math>)</code>

Graphic Functions

crude graph of $expr$ between $a$ and $b$	<code>plot(<math>X = a, b, expr</math>)</code>
High-resolution plot (immediate plot)	
plot $expr$ between $a$ and $b$	<code>plotoh(<math>X = a, b, expr, \{flag\}, \{n\}</math>)</code>
plot points given by lists $lx, ly$	<code>plotthraw(<math>lx, ly, \{flag\}</math>)</code>
terminal dimensions	<code>plotsizes()</code>

Rectwindow functions

init window $w$ , with size $x, y$	<code>plotinit(<math>w, x, y</math>)</code>
erase window $w$	<code>plotkill(<math>w</math>)</code>
copy $w$ to $w_2$ with offset $(dx, dy)$	<code>plotcopy(<math>w, w_2, dx, dy</math>)</code>
scale contents of $w$	<code>plotclip(<math>w</math>)</code>
scale coordinates in $w$	<code>plotscale(<math>w, x_1, x_2, y_1, y_2</math>)</code>
plotoh in $w$	<code>plotrecth(<math>w, X = a, b, expr, \{flag\}, \{n\}</math>)</code>
plotthraw in $w$	<code>plotrectthraw(<math>w, data, \{flag\}</math>)</code>
draw window $w_1$ at $(x_1, y_1), \dots$	<code>plotdraw([<math>w_1, x_1, y_1], \dots]</math>)</code>

Low-level Rectwindow Functions

set current drawing color in $w$ to $c$	<code>plotcolor(<math>w, c</math>)</code>
current position of cursor in $w$	<code>plotcursor(<math>w</math>)</code>
write $s$ at cursor's position	<code>plotstring(<math>w, s</math>)</code>
move cursor to $(x, y)$	<code>plotmove(<math>w, x, y</math>)</code>
move cursor to $(x + dx, y + dy)$	<code>plotrmove(<math>w, dx, dy</math>)</code>
draw a box to $(x_2, y_2)$	<code>plotbox(<math>w, x_2, y_2</math>)</code>
draw a box to $(x + dx, y + dy)$	<code>plotrbox(<math>w, dx, dy</math>)</code>
draw polygon	<code>plotlines(<math>w, lx, ly, \{flag\}</math>)</code>
draw points	<code>plotpoints(<math>w, lx, ly</math>)</code>
draw line to $(x + dx, y + dy)$	<code>plotrline(<math>w, dx, dy</math>)</code>
draw point $(x + dx, y + dy)$	<code>plotrpoint(<math>w, dx, dy</math>)</code>

Convert to Postscript or Scalable Vector Graphics

The format $f$ is either "ps" or "svg".	
as plotoh	<code>plotexport(<math>f, X = a, b, expr, \{flag\}, \{n\}</math>)</code>
as plotthraw	<code>plotthrawexport(<math>f, lx, ly, \{flag\}</math>)</code>
as plotdraw	<code>plotexport(<math>f, [[w_1, x_1, y_1], \dots]</math>)</code>

Based on an earlier version by Joseph H. Silverman  
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Send comments and corrections to (Karim.Belabas@math.u-bordeaux.fr)